

Calcul Téléportation.

$$|\phi\rangle_1 = \alpha|0\rangle_1 + \beta|1\rangle_1$$

$$\left(|\beta_{01}\rangle_{12} \langle\beta_{01}| \otimes I_3 \right) \left(|\phi\rangle_1 \otimes |\beta_{00}\rangle_{23} \right)$$

$$= |\beta_{01}\rangle_{12} \left(\frac{{}_{12}\langle 01| + {}_{12}\langle 10|}}{\sqrt{2}} \right) \otimes \left(|0\rangle_3 \langle 01| + |1\rangle_3 \langle 11| \right)$$
$$\left(\alpha|0\rangle_1 + \beta|1\rangle_1 \right) \otimes \left(\frac{|00\rangle_{23} + |11\rangle_{23}}{\sqrt{2}} \right)$$

$$= |\beta_{01}\rangle_{12} \left(\alpha \langle 11| + \beta \langle 10| \right) \otimes \left(|0\rangle_3 \langle 01| + |1\rangle_3 \langle 11| \right)$$
$$\otimes \left(\frac{|00\rangle_{23} + |11\rangle_{23}}{\sqrt{2}} \right)$$

$$= |\beta_{01}\rangle_{12} \left(\alpha \langle 11| + \beta \langle 10| \right) \otimes \left(\frac{|0\rangle_2 \otimes |0\rangle_3 + |1\rangle_2 \otimes |1\rangle_3}{\sqrt{2}} \right)$$

$$= |\beta_{01}\rangle_{12} \otimes \left(\alpha |1\rangle_3 + \beta |0\rangle_3 \right)$$

$$= |\beta_{01}\rangle_{12} \otimes \left(\beta |0\rangle_3 + \alpha |1\rangle_3 \right)$$

$$X|\phi\rangle_3 \quad \text{ou} \quad X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

(pink NOT)