

PROBLEM 1. Break the following ciphertexts which have been encrypted using a monoalphabetic substitution which rotates the letters of the alphabet k positions.

(a) UWTUJWYD NX F SZNXFSHJ.

(b) YGCMPGUU QH CVKVVWFG DGEQOGU YGCMPGUU QH EJCTCEVGT

The first sentence is a famous quote of the mathematician Paul Erdos and the second sentence is a famous quote of Albert Einstein. Figure out what they had to say.

PROBLEM 2. The plaintext "school" is encrypted as "KKNBOW".

(a) Was the cipher a monoalphabetic or polyalphabetic cipher (Vignere cipher) ?

(b) Which key was used ?

PROBLEM 3. Decrypt the ciphertext "EIUEEBERINTSFNEAVEAVTEOEHAEHOTG-TEEBEGANOWPSWRHOHACCATWTHFOIEOTIC" obtained by transposition with the key CUP OF TEA.

PROBLEM 4. (a) Prove that $\gcd(a, b) = \gcd(a, b + ca)$ for any integer c .

(b) Prove that $\gcd(a, b) = \gcd(a, b) = \gcd(5a + 2b, b + 2a)$.

(c) Prove that $\gcd(ma, mb) = m \cdot \gcd(a, b)$ where m is a non-negative integer.

(d) Prove that $\gcd(a, p) = 1$ or p with p a prime number.

PROBLEM 5. 1. Find the $\gcd(144, 60)$

2. Find two integers α, β such that $\gcd(144, 60) = 60\alpha + 144\beta$.